

**Embedded
Code Generation**
DEMO MODEL

LLC Resonant Converter

Control of an LLC resonant converter with time-scaling and embedded code generation for TI C2000 MCUs

Last updated in C2000 TSP 1.5.1

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1 Overview

The half-bridge LLC resonant converter is an attractive topology for DC/DC converters in applications such as battery chargers and power supplies, as it allows for zero voltage switching (ZVS) over a wide range of operating conditions resulting in comparatively low switching losses, high efficiency, and high power density.

This demo model highlights a variable switching frequency control approach for the LLC converter using a Texas Instruments (TI) C2000 microcontroller (MCU). The MCU runs embedded code generated from a PLECS model. The power stage for the model is based on the TI LLC Resonant Half-Bridge Converter 300 W Evaluation Module [1].

Hardware-in-the-Loop (HIL) testing is used to evaluate the controller performance. The plant model is optimized to run on the PLECS RT Box. Use of the Half-Bridge LLC Resonant Converter power module from the PLECS library is key to obtain accurate real-time simulations with the high switching frequencies in this application.

The model also incorporates time-scaling for HIL testing, where the RT Box and controller are both configured to model the system at a rate slower than real time. Time-scaling allows one to perform HIL testing on models that would otherwise have a processor load of over 100%, at the cost of not running the model in true real time.

Note This model contains model initialization commands that are accessible from:

PLECS Standalone: The menu **Simulation + Simulation Parameters... + Initializations**

PLECS Blockset: Right click in the **Simulink model window + Model Properties + Callbacks + InitFcn***

2 Model

The top-level schematic contains two separate subsystems representing the controller and plant models, as shown in Fig. 1. Both subsystems are enabled for code generation from the **Edit + Subsystem + Execution settings...** menu. This step is necessary to generate the model code for a subsystem via the PLECS Coder.

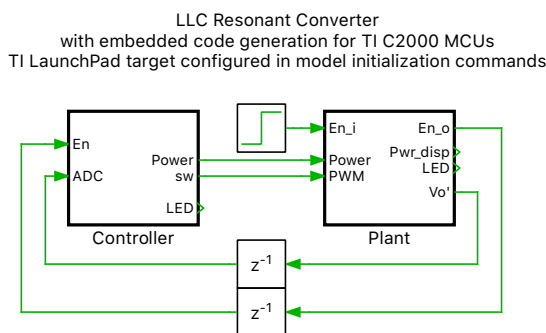


Figure 1: Top-level schematic of the plant and the controller subsystems

2.1 Power Circuit

The power stage for the model is shown Fig. 2. The design is based on the TI LLC Resonant Half-Bridge Converter 300 W Evaluation Module which has a 390 V input and a regulated 12 V output.

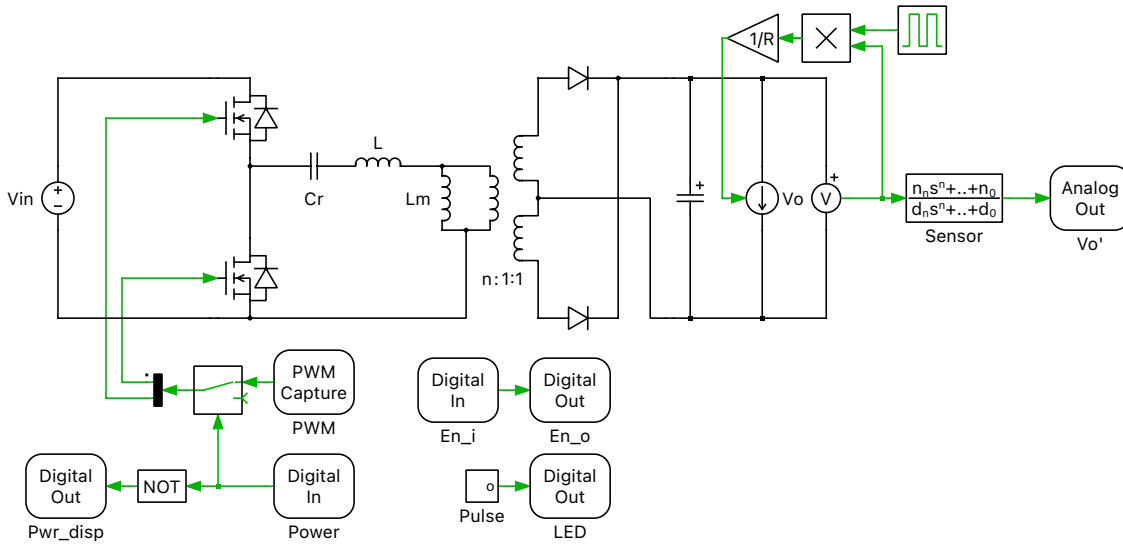


Figure 2: Plant model optimized for the RT Box

Theory of operation

In the LLC converter the half-bridge is typically modulated to generate a square-wave voltage signal at the input of the resonant tank. The resonant tank consists of a series resonant inductance L_r , a magnetizing inductance L_m , and a resonant capacitor C_r . The upper and lower switching elements are modulated in a complementary fashion (with an appropriate dead-time) and typically at 50% duty. The square-wave voltage input results in a quasi-sinusoidal current flowing within the resonant network. An output transformer, rectifier circuit, and filter establish a DC output voltage from the sinusoidal tank currents.

Changing the frequency of the square-wave voltage input from the half-bridge changes the effective impedance of the resonant tank, and therefore the resulting current output. Assuming a gain M from the resonant tank, the relationship between the input and output voltage is:

$$V_o = M \frac{1}{n} \frac{V_{in}}{2}$$

The series resonant frequency of the LLC converter, f_0 , is the point where the L_r and C_r combination have zero impedance and the gain M is unity (in a lossless circuit). Typically the converter will operate near f_0 .

$$f_0 = \frac{1}{2\pi\sqrt{L_r C_r}}$$

However, the gain depends not only the switching frequency and tank design, but also the converter load resistance R_o . The DC output resistance R_o can be approximated by an equivalent AC load resistance R_e [2]. R_e is used to calculate the quality factor Q_e , which defines how the resonant gain changes as a function of frequency.

$$R_e = \frac{8n^2}{\pi^2} R_o \text{ and } Q_e = \frac{1}{R_e} \sqrt{\frac{L_r}{C_r}}$$

Fig. 3 shows a series of curves highlighting how the switching frequency and quality factor impact the gain of a lossless converter. For the power stage in this model, $Q_e = 0.41$ at rated load and the resonant frequency is $f_0 = 138.5 \text{ kHz}$. [1]. The frequency axis is normalized such that $f_n = f_{sw}/f_0$.

In Fig. 3 the ϕ_2 curve shows the point where the phase of the resonant circuit is zero, indicating a transition from a capacitive current in the resonant tank at lower frequencies to an inductive current at higher frequencies. Maintaining an inductive current is essential to achieve ZVS on the primary half-bridge. This also maintains a consistent relationship where increasing the converter switching frequency results in a decreased voltage gain.

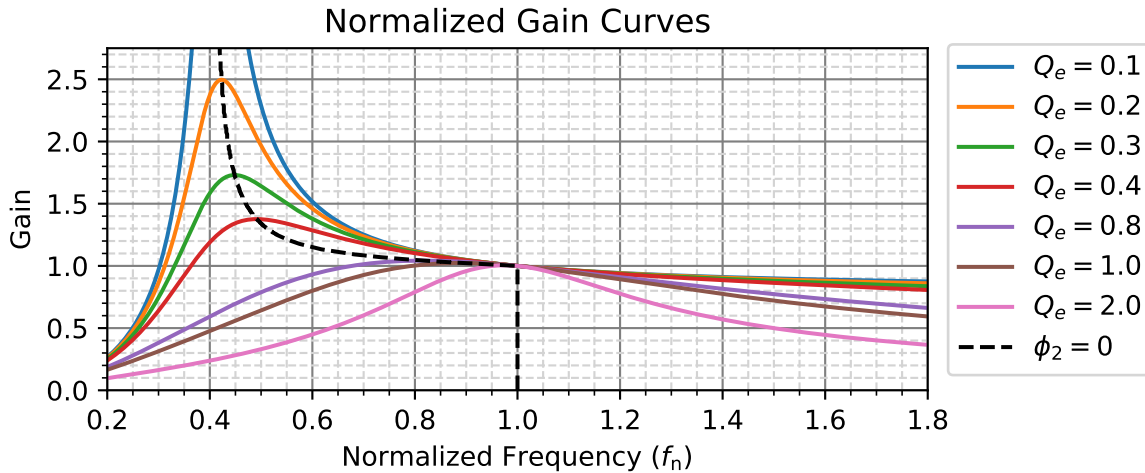


Figure 3: Normalized gain curves for the converter

The Half-Bridge Resonant LLC Converter power module

The Half-Bridge LLC Resonant Converter power module component incorporates the half-bridge MOSFET input, the resonant tank, high frequency transformer, and output rectification. The component values are entered in the block mask. When the power module is configured as Switched, the LLC is implemented fully in the electrical domain, with the power semiconductors modeled with ideal switches. When the Sub-step events configuration is chosen the power module is implemented with controlled current sources at both the input and output terminals, as opposed to using ideal switches. The control signal inputs to the half-bridge in the Sub-step events configuration are the average on-time of the switching elements, with values between 0 and 1.

The “Sub-step events” implementation is an extension of the “Sub-cycle average” concept [3], which yields more accurate simulation results than a purely switched model when discretized at a given step size. Sub-step calculations occur within one simulation step, which results in the calculation of as many inductors current values as switching combinations encountered during one simulation step. This approach allows for a more accurate calculation of the average inductor currents, which is critical to obtain an accurate capacitor voltage calculation.

RT Box configuration

The PWM Capture block configures the RT Box to sense the MOSFET gate signals from the MCU, as shown in Fig. 2. The output of the PWM Capture component provides the average on-time duration for each switch over the previous model step, where the model step duration is less than the switching period. The Half-Bridge LLC Resonant Converter power module gate inputs utilize the averaged on-time values, the input and output voltages, and the state of the energy storage elements to compute the average inductor currents, capacitor voltage, and associated network current injections.

A voltage-controlled current source is used to model a variable load. In this case, the effective output resistance is controlled by a Pulse Generator that toggles the output resistance between full load and half load. The variable load provides a disturbance which is used to evaluate the controller performance. A delay equal to one model-step is introduced in this feedback loop due to a zero-order hold included in the controlled current source. A first-order low-pass filter is used to represent the output voltage sensing circuit in the LLC hardware. The sensed converter output voltage is then routed to an RT Box analog output channel.

Additional digital signals are used so the user can enable or disable the controller and power stage through the use of an external status switch.

The plant real-time model is time-scaled to execute at $1/10^{\text{th}}$ of real time with an effective discretization size of $0.4\ \mu\text{s}$, resulting in an actual step size of $4.0\ \mu\text{s}$. Time-scaling is explained in more detail in Section 2.3.

2.2 Controls

Fig. 4 shows a high-level overview of the control logic for the TI C2000 MCU.

The controller senses the input voltage via the analog-to-digital converter (ADC) and regulates the output voltage of the LLC converter by changing the switching frequency of the PWM output. Additionally, there is a manual signal switch so the converter can be operated at a user-specified fixed frequency, bypassing the regulator. The output of the compensator and the “Fixed Frequency” value are normalized to the series resonant frequency, f_0 . The output is then limited to be in the expected operating range, such that at rated maximum load the converter will retain ZVS, and is scaled to generate the desired switching frequency.

The description of the controls below is based on the operation with real power hardware in true real time. Similar to the RT Box, for HIL testing the execution of the control loop is time-scaled to $1/10^{\text{th}}$ of real time as described in Section 2.3.

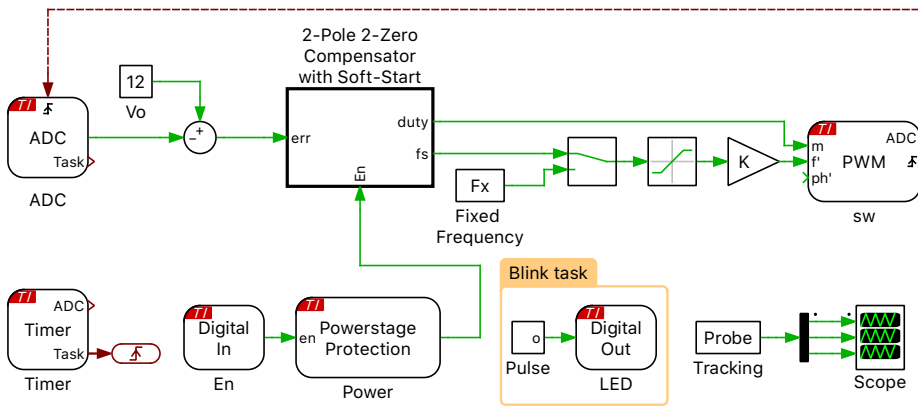


Figure 4: Overview of the embedded controller logic

Control architecture

Fig. 5 shows the implementation of the compensator and soft-start mechanism. A State Machine is used to begin the soft-start sequence whenever the “En” input transitions from low to high. The State Machine inputs are triggers indicating the status of the soft-start actions. Outputs of the State Machine are used to control three different Enabled Subsystems, only one of which is active at a given time. The advantage of using the Enabled Subsystem is that when the enable input is low, the logic within the subsystem does not execute, reducing the computational load on the MCU.

The soft-start sequence begins from a switching frequency 1.5 times greater than the expected final operating point at the rated load. This ensures operation on the ZVS portion of the curve during soft start and a lower output voltage to prevent excessive gain under light-load conditions. With the frequency still fixed, the duty cycle is then linearly ramped from 0% to 50% duty over a fixed time period. A trigger signal is generated by the “Duty Cycle Soft Start” component to initiate the frequency soft-start mechanism. Next, the switching frequency is linearly ramped downwards to the expected final switching frequency. The “Frequency Soft Start” component sends a trigger upon completion that activates the “Frequency Control” subsystem, which contains a two-pole two-zero (2P2Z) compensator. If the sequence is aborted at any point by a logical low “En” input, the sequence starts again from the beginning.

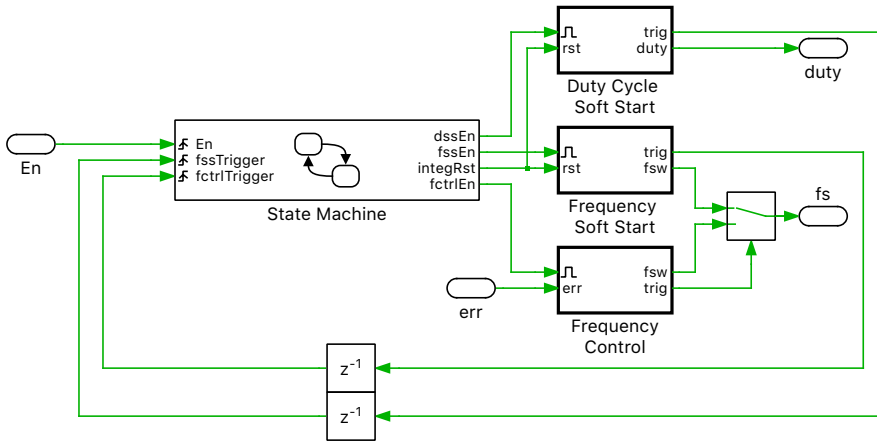


Figure 5: Controller soft-start implementation

The 2P2Z compensator is implemented as a Direct Form-I digital compensator with an output limitation, as shown in Fig. 6. The controller parameters are determined by first using Extended Describing Functions to obtain the plant transfer function, then pole-zero matching is used to design a controller in the continuous domain, and lastly the continuous controller is discretized [4]. The crossover frequency is 2 kHz in the final design.

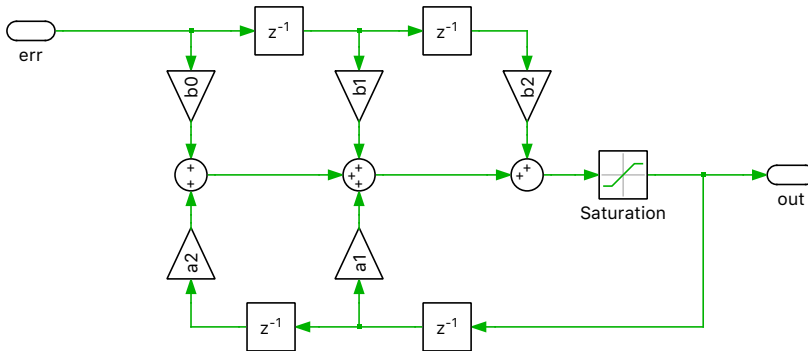


Figure 6: Two-pole two-zero (2P2Z) discrete implementation

Configuring TI C2000 Target library components

The schematic in Fig. 4 contains several components from the TI C2000 Target library. The PWM (Variable) component is used to generate a variable-frequency PWM signal. The input to the block, “f” is normalized to the **Carrier frequency** parameter in the component mask of 110 kHz. The PWM (Variable) block is configured to generate the start-of-conversion (SOC) signal for the ADC. From the **Events** tab of the PWM block parameter window, the **ADC Trigger** parameter is configured as Underflow. Then the **Trigger source** parameter of the ADC block is set to “Show trigger port”. The trigger signal is shown as a red dashed line connecting the PWM and ADC components.

The Timer component generates an interrupt at a fixed rate of half the nominal carrier frequency of the PWM (Variable) component, or 55 kHz. The Timer’s Task output triggers the control task, which is asynchronous to the PWM generation and ADC sampling. The control task uses the most recent ADC measurement when calculating the compensator response. Executing the control task at a fixed rate ensures the discrete 2P2Z compensator and other model calculations are appropriately discretized. Having the PWM trigger the ADC SOC ensures consistent point-on-wave sampling of the voltage measurement.

In order to enable or disable PWM signals during runtime, DIP switch “DI-29” on the RT Box LaunchPad Interface board is used. This input signal “DI-29” is connected to the Digital In block labeled “En_i” in the “Plant” subsystem, which is then routed as the input of the Powerstage Protection block on the “Controller” subsystem through the RT Box LaunchPad Interface board. The Powerstage Protection block implements a finite state machine to enable or disable all PWM outputs on the target MCU. A logic low to high transition enables the PWM outputs, while a high to low transition disables them. The output of the Powerstage Protection block also enables the compensator and soft-start logic. For more details, please browse the **Help** section of this block.

When the power stage is enabled, a digital output, configured in the **Powerstage enable GPIO number** of the Powerstage Protection block, is toggled. This signal is connected to the Digital In block labeled “Power” in the “Plant” subsystem. A Signal Selector component is used to model a gate driver. When the “Power” input is logical low the half-bridge gate signals are all zero. Once the “Power” input is logical high, then the switch connects the signals from the “PWM” input to the MOSFET gate signals. With the “Power” logical high, the red LED “DO-29” on the LaunchPad Interface board will also turn on, visually indicating the switching signals are connected to the MOSFET gates.

2.3 Time-Scaling Concepts

Real-time simulation involves a trade-off between model complexity and model fidelity. As a model becomes more numerically complex it naturally takes a longer time to compute. Similarly, if a very short discretization step size is required to meet the model fidelity requirements, a limited amount of time is available for the processor to compute the model results in real time. At a certain point the execution time of the model may exceed the required discretization time step.

Time-scaling is one approach to overcome this limitation, where the execution of the RT Box plant model and the embedded controller are both slowed, in lock-step, as compared to real time. If the model is time-scaled to run at $1/10^{\text{th}}$ of real time, then a 1 second event would occur over 10 seconds in a time-scaled model. Through careful manipulation of the RT Box parameters the “dynamics” of the model are retained, but the RT Box has additional time to perform the necessary calculations.

If we consider a time-scaling factor K_{scale} where $K_{\text{scale}} < 1$ corresponds to slower than real time, then to time-scale the LLC plant model for the RT Box, all inductances, capacitances, and time constants are divided by K_{scale} . Frequencies are multiplied by K_{scale} . One could consider this as changing all L/R and $1/(RC)$ time constants in the electrical circuit by a common factor. The model discretization step size is divided by K_{scale} as well.

Changes to the controller are also required. When using the TI C2000 TSP, the Timer “Frequency” setting and PWM “Carrier frequency” are multiplied by K_{scale} to increase the control task and PWM periods. Note that the 2P2Z compensator parameters do not change. The delays in the compensator implementation, as shown in Fig. 6, are set equal to one control task period. By changing the control task period, the dynamics of the compensator are automatically scaled appropriately.

If the MCU code is hand-written, then comparable changes are required. While time-scaling does require altering the controller software, minimal changes to the code-base allow one to test the embedded controller in conjunction with the RT Box with a high-fidelity plant model. Then, when the controller is interfaced with real hardware the modifications required for time-scaling would be removed.

3 Simulation

The simulation model can be run offline on a desktop computer by choosing the **Simulation + Start** menu option.

Fig. 7 shows the results from the “Controller” subsystem highlighting the startup sequence without time-scaling and an $0.4 \mu\text{s}$ discretization step size for the plant model. At 1 ms the controller is enabled and the soft-start sequence begins. The output duty begins to increase from 0 % to 50% over 5 ms while the frequency is held constant. Then the frequency begins to ramp over the next 5 ms to

the expected final operating point of $\sim 0.83f_0$. At 11 ms the 2P2Z compensator is activated and the output voltage is regulated to 12 V.

Step changes in the output load are visible at 20 ms and 40 ms resulting in brief voltage transients, as highlighted in Fig. 8

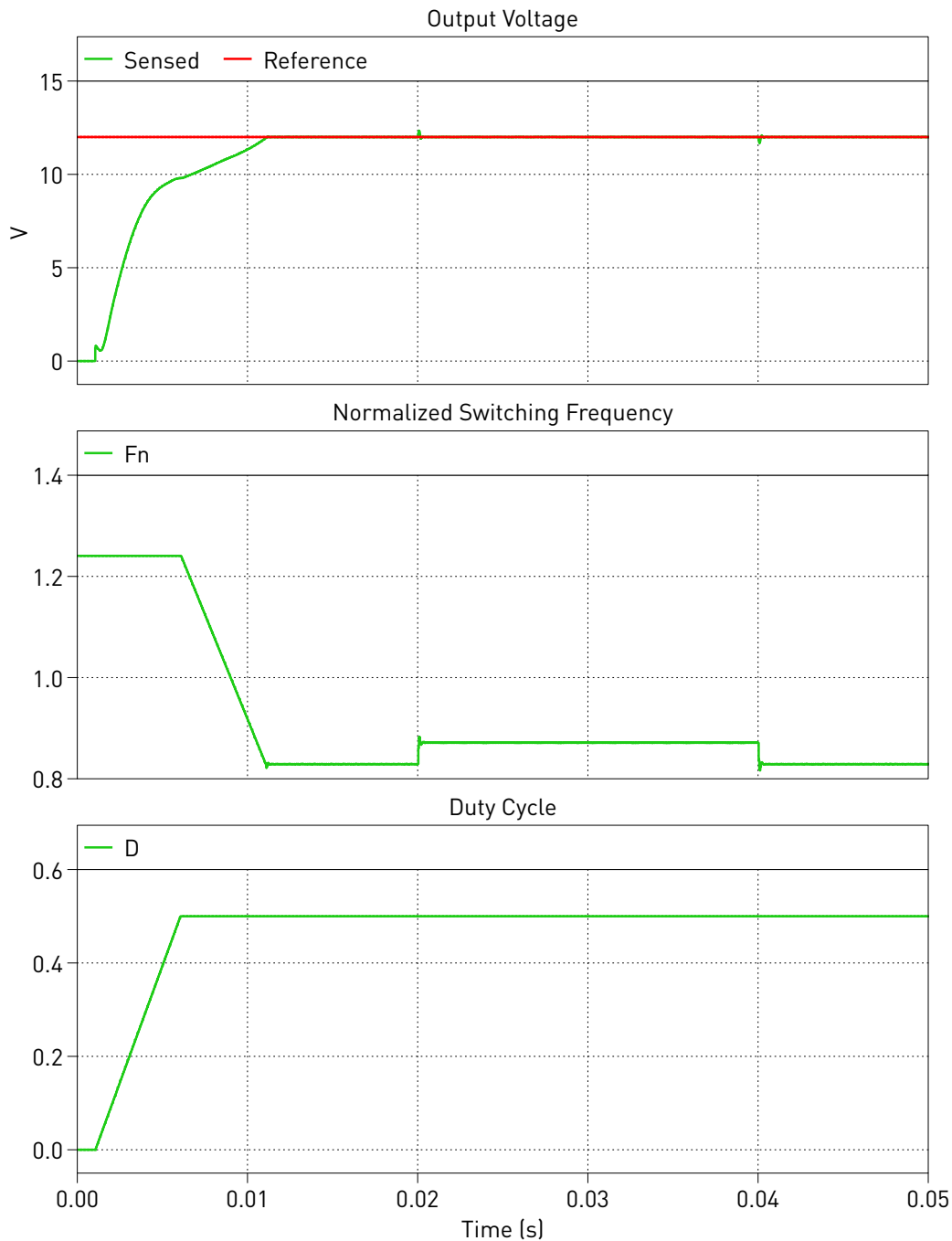


Figure 7: Controller performance during startup without time-scaling

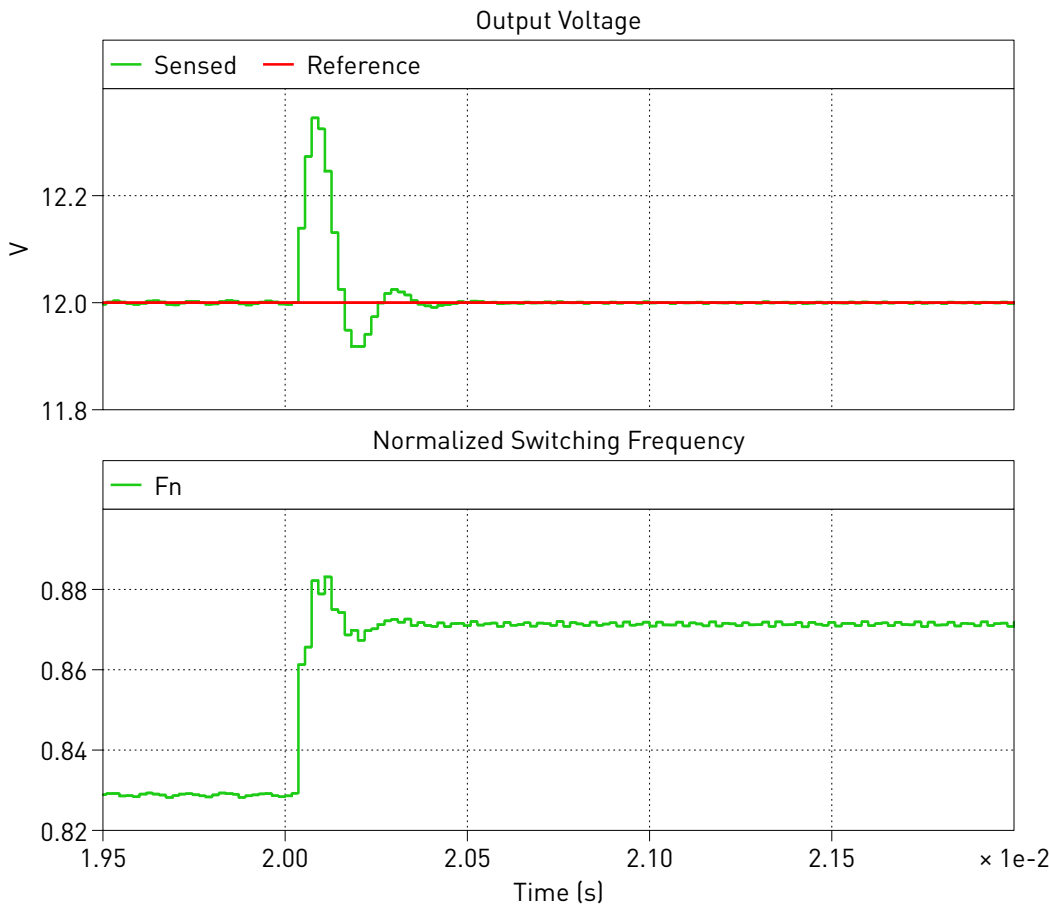


Figure 8: Controller performance during transient without time-scaling

3.1 Application of Time-Scaling

Fig. 9 shows the benchmarking of a full switching model with a variable-step solver, labeled “Switched”, against the discretized Sub-step event configurations of the LLC model, labeled as “SSE”. The Sub-step event models are discretized at $1.2\ \mu\text{s}$ and $0.4\ \mu\text{s}$. A step size of $1.2\ \mu\text{s}$ was selected as a representative value greater than the $1\ \mu\text{s}$ minimum step size of the RT Box hardware, although the processor load may still exceed 100%. There is no time-scaling applied in Fig. 9.

The scaling parameter is defined in the **Model initialization commands** accessed from the **Initialization** tab of **Simulation + Simulation parameters** dropdown menu. The scale value is set to `scale=1.0` and the plant discretization step size is set to `Ts_plant=1.2e-6/scale` and `Ts_plant=0.4e-6/scale` to generate Fig. 9.

While the output voltage in steady state is regulated to 12V in all cases, a deviation is apparent in the startup voltage for the Sub-step events results discretized at $1.2\ \mu\text{s}$. Additionally there is an offset in the regulator output frequency for the model discretized at $1.2\ \mu\text{s}$ of $\sim 6.7\%$. Similarly, if the model were run at a fixed switching frequency an error in the LLC output voltage would be apparent.

The RT Box hardware does not allow for discretization step sizes less than $1\ \mu\text{s}$. In order to achieve the fidelity of the Sub-step event model with a $0.4\ \mu\text{s}$ step size, time-scaling is required.

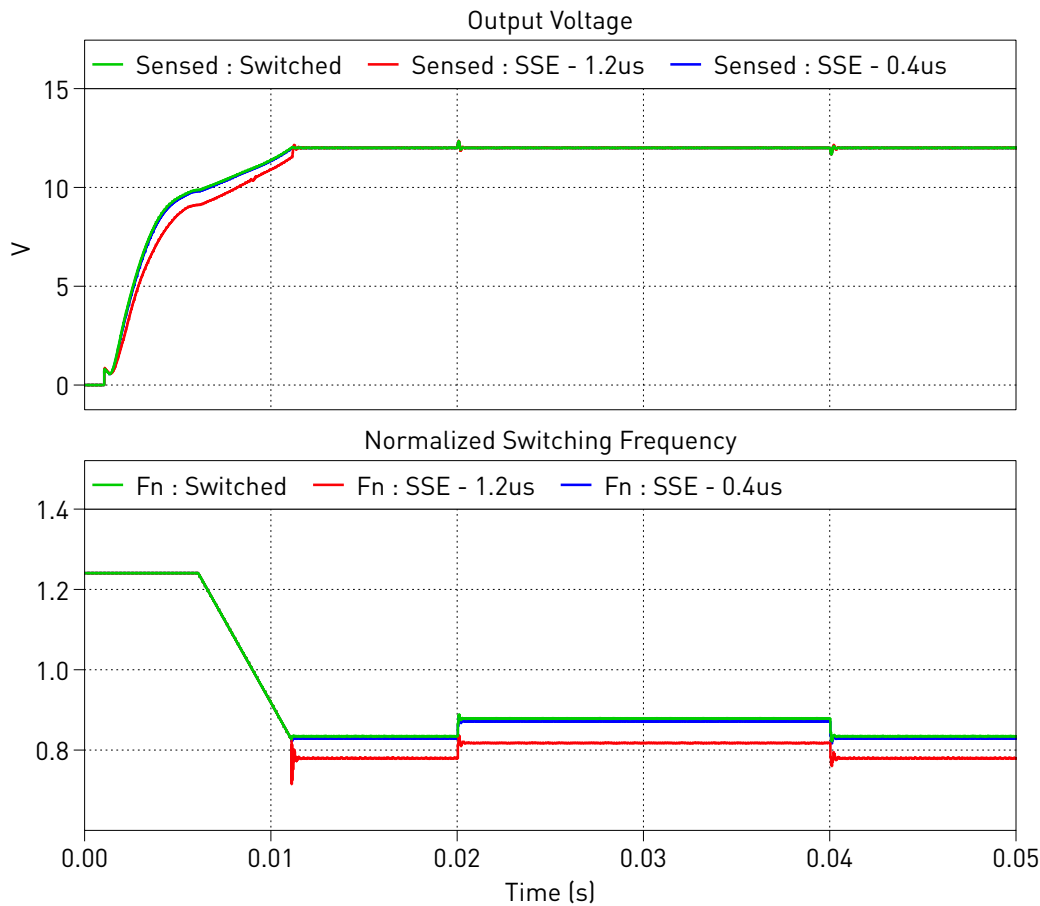


Figure 9: Comparing Sub-step event results with the Switched solution without time-scaling

To discretize the model at an effective step size of $0.4\ \mu\text{s}$ and time-scaled to execute at $1/10^{\text{th}}$ of real time change the scale value to $\text{scale}=0.1$ and set $\text{Ts_controller}=0.4\text{e-}6/\text{scale}$. Now each simulation step will have $4\ \mu\text{s}$ to compute on the RT Box, significantly reducing the processor load (or ratio of calculation time to model step size).

Fig. 10 shows the results of the time-scaled simulation for the switched model and Sub-step events model at different discretization step sizes. The time-scaled Sub-step events models run on the RT Box at $4\ \mu\text{s}$ and $12\ \mu\text{s}$ with low RT Box processor loads. Note that the time axis of Fig. 10 has a maximum value of $0.50\ \text{s}$ and the non-scaled results in Fig. 9 show a maximum time axis value of $0.05\ \text{s}$. Fig. 11 shows a close-up of the system response during a step decrease in load, which can be compared with the non-scaled results in Fig. 8. Again, note the difference in the time axis values.

If one were to down-sample the time-scaled results by a factor of 10, or divide the time-axis by 10, and overlay the time-scaled and non-scaled plots, the traces would be near-identical.

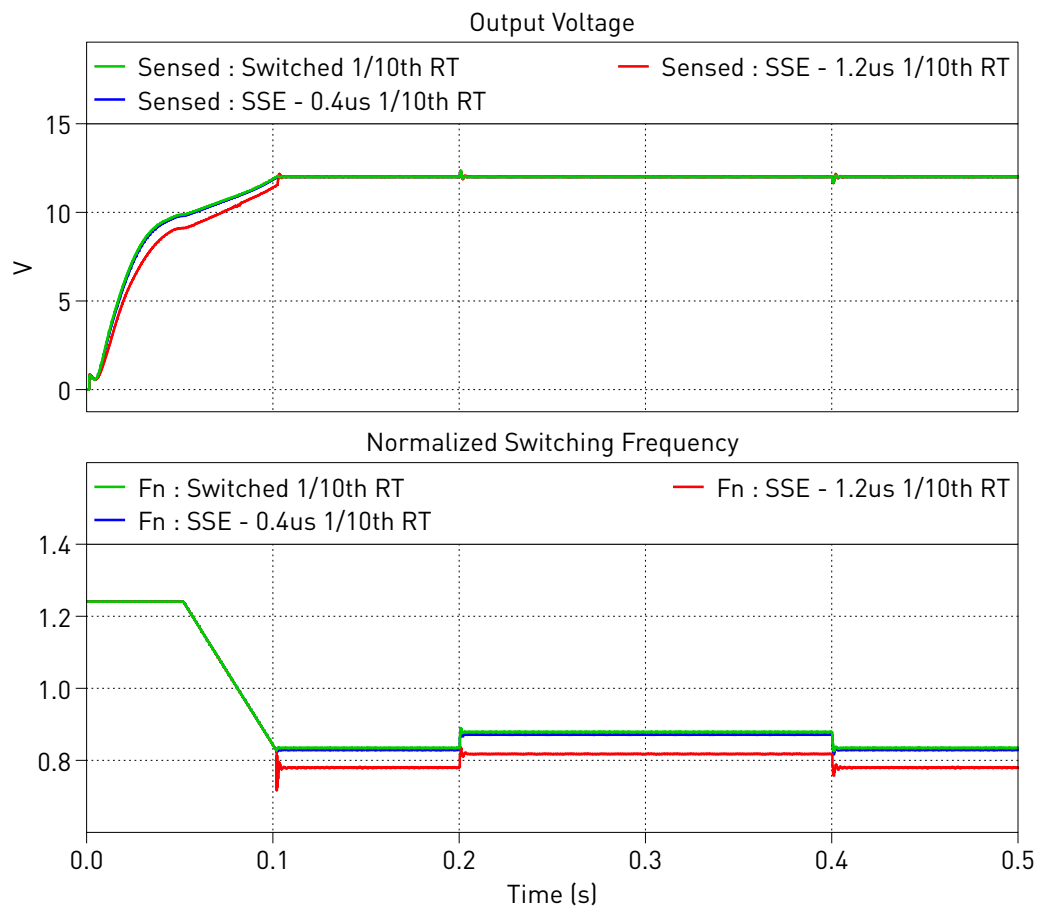


Figure 10: Sub-step event and Switched model comparison during startup at 1/10th real time

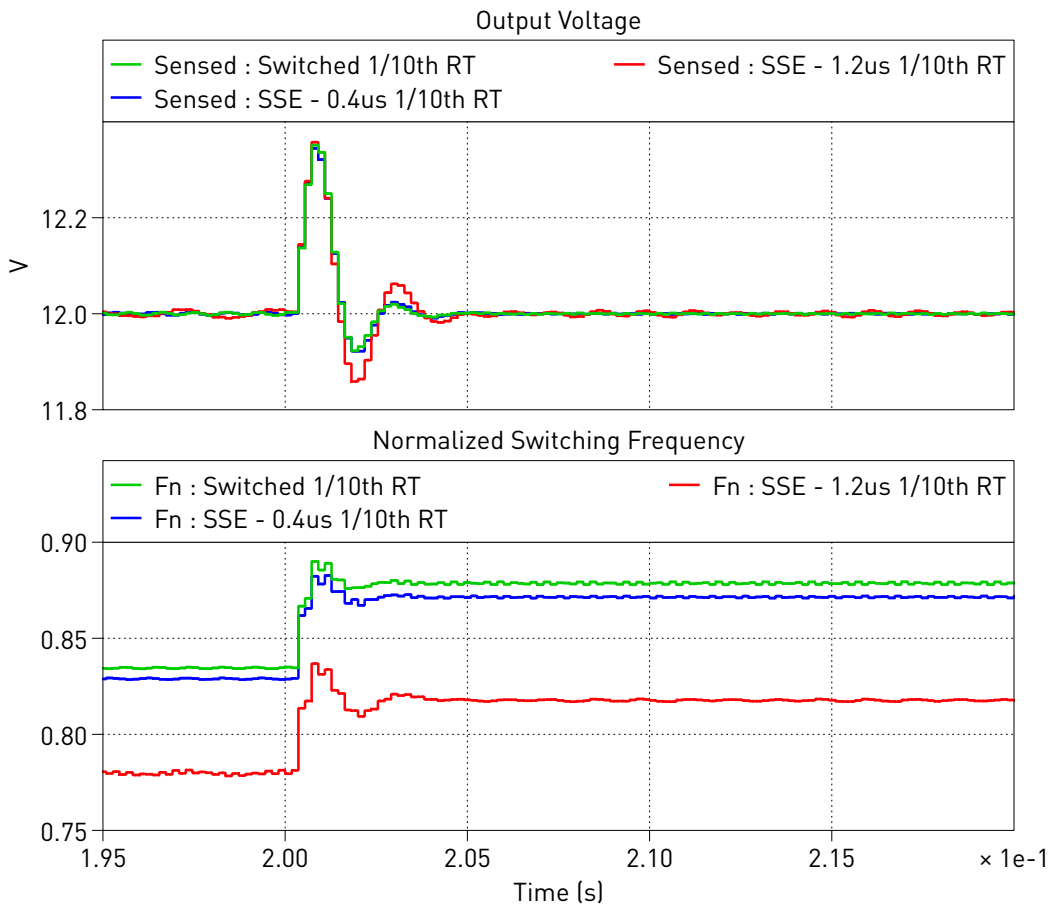


Figure 11: Sub-step event and Switched model comparison during transient at 1/10th real time

3.2 Configuring the TI C2000 Target

In addition to running a simulation of this demo model in offline mode on a computer, the “Controller” subsystem can be directly converted into target specific code for the TI LaunchPads. The model is configured by default for a TI 28379D LaunchPad [5], but the TI 28377S [6] and 28388D [7] are also supported as explained later in this section.

Follow the instructions below to upload the “Controller” subsystem to a TI MCU.

- Connect the MCU to the host computer through a USB cable.
- From the **System** tab of the **Coder + Coder options...** window, select “Controller”.
- Next, from the **Target** tab, select the appropriate target from the dropdown menu. Then under the **General** sub-tab, select the desired **Build type**.
- Then, to Build and program the MCU directly from PLECS, choose either Run from Flash or Run from RAM as the **Build configuration** to program the MCU either to flash memory or to RAM respectively, then select LaunchPad as the **Board type**, and click **Build**.

If programmed correctly, LED “D9” (or the LED corresponding to GPIO “DO_DSP_LED” listed in the model initialization commands) should blink.

For advanced users who are familiar with Code Composer Studio, there is an option to Generate code into CCS project. Locate the appropriate cg folder from the CCS project (refer to [9] for step-by-step instructions), enter its path into the **CCS project directory** field and click **Build**. The code of the “Controller” subsystem will be automatically generated. Then, proceed to build and debug the project as a normal CCS project.

Please note that the I/O configuration of all the peripheral blocks (ADC, PWM) are configured by mapping to the TI 28379D LaunchPad [5]. For a TI MCU other than the TI 28379D LaunchPad, the I/O configuration has to be adapted. This demo model also supports code generation for the TI 28377S [6] LaunchPad; as well as the TI 28379D [8] and TI 28388D [7] controlCARDs. From the **Model initialization commands** window of **Simulation Parameters... + Initializations** tab from the **Simulation** menu, change the value of `type_evm`, to choose the desired target. You must also configure the corresponding **Target** in the **Coder Options** window accordingly.

Note If using the RT Box LaunchPad Interface board, make sure that the **RST** jumper is open throughout the simulation.

3.3 Configuring the PLECS RT Box

Prior to controlling a real power stage with the programmed MCU, it is highly recommended to first verify the behavior of the controller using a PLECS RT Box and perform a hardware-in-the-loop (HIL) test. A typical hardware configuration is shown in Fig. 12, where the evaluation kit, a TI 28379D LaunchPad (the red board), is connected to the RT Box via an RT Box LaunchPad Interface (the green board).

Follow the instructions below to run a real-time model on the RT Box.

- From the **System** tab of the **Coder + Coder options...** window, select “Plant”. Click the **Target** tab and select a target device. Then click **Build** to deploy the model to the target RT Box.
- Once the model is uploaded, from the **External Mode** tab of the **Coder options...** window, **Connect** to the RT Box and **Activate autotriggering** to observe the test results in real time.

If programmed correctly, the LED corresponding to “DO-31” of the RT Box LaunchPad Interface board should blink.

Toggle the switch “DI-29” on the RT Box LaunchPad Interface board from low to high to enable the MCU, as explained at the end of Section 2.2. When the power stage is enabled, the LED corresponding to “DO-29” of the LaunchPad interface board should turn on. Observe the real-time waveforms in the Scope of the “Plant” subsystem.



Figure 12: Hardware setup of the HIL verification with the RT Box

Note At this stage, verify that the LED corresponding to “DO-29” on the RT Box LaunchPad Interface board is turned on.

3.4 Starting the Controller and Connecting via the External Mode

Toggling the switch “DI-29” on the RT Box LaunchPad Interface board from high to low should disable all the gating signals. The “DO-29” LED indicator on the LaunchPad Interface board will be off. Toggling “DI-29” back to high will enable the PWM outputs once again and the “DO-29” LED will turn on.

In order to tune the parameters of the control program in the MCU and observe any intermediate values, follow the instructions below to connect to the external mode of the TI MCU.

- First, **Disconnect** the “Plant” subsystem from the **External Mode** of the PLECS RT Box, if connected.
- Then, from the **System** menu on the left hand side of the **Coder + Coder options...** window, select “Controller”.
- Next, from the **External Mode** tab, select the appropriate **Target device** and click **Connect**.
- Then, **Activate autotriggering** to observe the test results in the “Controller” subsystem Scope.

Once connected, it is possible to change the voltage reference for the closed-loop controller, or to click the manual signal switch and operate in a fixed-frequency mode. The “Fixed Frequency” value can be changed in real time to see how the plant responds to changes in the switching frequency and load changes.

One may also observe the startup sequence by configuring the External Mode to trigger on an appropriate signal, for example the rising edge of the Duty Cycle crossing 1 %. The **Trigger channel** is set in the **External Mode** tab.

4 Conclusion

This model demonstrates the closed-loop control of a half-bridge LLC resonant converter using embedded code generation for TI C2000 MCUs. It can be run in both offline mode, as well as in real time. The controller features a soft-start mechanism and a discrete implementation of a 2P2Z compensator. Time-scaling was used to further enhance the model fidelity for HIL testing.

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- [6] TI C2000 Delfino MCU F28377S LaunchPad development kit,
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- [7] TI C2000 F28388D controlCARD evaluation module,
URL: <https://www.ti.com/tool/TMDSCNCD28388D>.
- [8] TI C2000 F28379D controlCARD development kit,
URL: <https://www.ti.com/tool/TMDSCNCD28379D>.
- [9] PLECS TI C2000 Target Support User Manual,
URL: <https://www.plexim.com/download/documentation>.

Revision History:

C2000 TSP 1.2	First release
C2000 TSP 1.3.1	Turn on Assertions in the Half-Bridge LLC Resonant Converter power module
C2000 TSP 1.4.5	Updated the web links
C2000 TSP 1.5.1	Added support for 28388D and 28379D controlCARD targets

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Embedded Code Generation Demo Model

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